

5.6

$$t_f - t_0 = \int_{h_f}^{h_0} \frac{dh}{\frac{DV}{W}} = \int_{h_f}^{h_0} \frac{dh}{\frac{1}{2E^*} \left(u^2 + \frac{1}{u^2}\right) V^* u}$$

$$= 2E^* \int_{h_f}^{h_0} \frac{1}{V^*} \frac{dh}{u^3 + \frac{1}{u}}$$

$$\frac{\partial(t_f - t_0)}{\partial V} \Big|_{h = \text{const}} = 0 \Rightarrow \frac{\partial(t_f - t_0)}{\partial u} \Big|_{h = \text{const}} = 0$$

$$3u^2 - \frac{1}{u^2} = 0 \quad u = \frac{1}{\sqrt[4]{3}}$$

$$(t_f - t_0)_{\max} = 2E^* \int_{h_f}^{h_0} \sqrt{\frac{\rho S_w C_L^*}{2W}} \frac{dh}{\frac{\frac{1}{3} + 1}{\frac{1}{\sqrt[4]{3}}}} \quad \frac{\sqrt[4]{3}}{3}$$

$$= \cancel{2E^*} \sqrt{\frac{S_w C_L^*}{2W}} \frac{3}{\sqrt[4]{3}} \int_{h_f}^{h_0} \sqrt{\rho} dh$$

$$(t_f - t_0)_{\max} = \frac{E^*}{V_s^*} \frac{3}{2\sqrt[4]{3}} \int_{h_f}^{h_0} \sqrt{\sigma} dh$$

$$X_f - X_0 = \int_{h_f}^{h_0} \frac{dh}{D/W} = \int_{h_f}^{h_0} \frac{dh}{\frac{1}{2E^*} \left(u^2 + \frac{1}{u^2}\right)}$$

$$= 2E^* \frac{1}{\frac{4/3}{\sqrt[4]{3}}} (h_0 - h_f)$$

$$X_f - X_0 = \frac{\sqrt{3}}{2} E^* (h_0 - h_f)$$