

5.2 $T(\alpha, P) + P = \text{Const} \rightarrow T = \text{Const.}$

$$T - \frac{1}{2} C_{D0} \rho S_w V^2 - \frac{2KW^2}{\rho S_w V^2} = 0$$

$$\frac{1}{2} C_{D0} \rho^2 S_w^2 V^4 - T \rho S_w V^2 + 2KW^2 = 0$$

$$V^2 = \frac{T}{C_{D0} \rho S_w} \left[1 + \sqrt{1 - 4C_{D0} K \frac{W^2}{T^2}} \right] \text{ using the high-speed solution (+)}$$

$$\frac{1}{C_{D0}} = 2 \frac{E^*}{C_L^*} \quad 4C_{D0} K = \frac{1}{E^{*2}}$$

$$V^2 = \frac{2TE^*}{\rho S_w C_L^*} \left[1 + \sqrt{1 - \left(\frac{W}{TE^*}\right)^2} \right]$$

$$\frac{dx}{dW} = -\frac{V}{CT} \quad x_f - x_0 = \int_{W_f}^{W_0} \frac{V}{CT} dW$$

$$x_f - x_0 = \frac{1}{CT} \sqrt{\frac{2TE^*}{\rho S_w C_L^*}} \int_{W_f}^{W_0} \sqrt{1 + \sqrt{1 - \left(\frac{W}{TE^*}\right)^2}} dW \frac{TE^*}{TE^*}$$

$$\mu = \frac{W}{TE^*} \quad x_f - x_0 = \frac{E^*}{C_L} \sqrt{\frac{2TE^*}{\rho S_w C_L^*}} \int_{\mu_f}^{\mu_0} \sqrt{1 + \sqrt{1 - \mu^2}} d\mu$$

$$z = \sqrt{1 - \mu^2} \quad \mu = \sqrt{1 - z^2} \quad d\mu = -\frac{z dz}{\sqrt{1 - z^2}}$$

$$\begin{aligned} \text{Integral} &= - \int_{z_f}^{z_0} \frac{z dz}{\sqrt{1 - z^2}} = - \frac{2}{(-1)^2} \left[\frac{(1 - z)^{3/2}}{3} - (1 - z)^{1/2} \right]_{z_f}^{z_0} \\ &= \frac{2}{3} \left[\sqrt{1 - z} (2 + z) \right]_{z_f}^{z_0} = \frac{2}{3} \left[\sqrt{1 - \mu^2} (2 + \sqrt{1 - \mu^2}) \right]_{\mu_f}^{\mu_0} \end{aligned}$$

$$x_f - x_0 = \frac{2E^*}{3C} \sqrt{\frac{2TE^*}{\rho S_w C_L^*}} \left[A(W_0) - A(W_f) \right] \quad A = \sqrt{1 - \sqrt{1 - \left(\frac{W}{E^* T}\right)^2}} \left[2 + \sqrt{1 - \left(\frac{W}{E^* T}\right)^2} \right]$$

