

$$5.1 \quad L=W \Rightarrow V = \sqrt{\frac{2W}{\rho S_w C_L}} \quad C_L = \text{const.}$$

$$-\frac{dx}{dw} = \frac{V}{c_D} = \frac{E(C_L)}{c} \sqrt{\frac{2}{\rho S_w C_L}} \frac{1}{\sqrt{W}}$$

$$x_f - x_0 = \frac{2E(C_L)}{c} \sqrt{\frac{2}{\rho S_w C_L}} (\sqrt{W_0} - \sqrt{W_f})$$

$$-\frac{dt}{dw} = \frac{1}{c_D} = \frac{E(C_L)}{c} \frac{1}{W}$$

$$t_f - t_0 = \frac{E(C_L)}{c} \ln\left(\frac{W_0}{W_f}\right)$$

$$\max \frac{E}{\sqrt{C_L}} = \max \frac{\sqrt{C_L}}{C_{D0} + K C_L^2}$$

$$\frac{d}{dC_L} = 0 \quad (C_{D0} + K C_L^2) \frac{1}{2\sqrt{C_L}} - \sqrt{C_L} 2K C_L = 0$$

$$C_{D0} + K C_L^2 - 4K C_L^2 = 0 \Rightarrow C_L = \frac{1}{\sqrt{3}} \sqrt{\frac{C_{D0}}{K}} = \frac{C_L^*}{\sqrt{3}}$$

$$\left(\frac{E}{\sqrt{C_L}}\right)_{\max} = \frac{\frac{1}{3^{1/4}} \frac{C_{D0}^{1/4}}{K^{1/4}}}{C_{D0} + K \frac{C_{D0}}{3K}} = \frac{3^{3/4}}{4 K^{1/4} C_{D0}^{3/4}}$$

$$\max E \quad C_L = C_L^* \quad \frac{E}{\sqrt{C_L}} = \frac{E^*}{\sqrt{C_L^*}} = \frac{\left(\frac{C_{D0}}{K}\right)^{1/4}}{C_{D0} + K \frac{C_{D0}}{K}}$$

$$\frac{E^*}{\sqrt{C_L^*}} = \frac{1}{2 C_{D0}^{3/4} K^{1/4}}$$

$$\frac{\frac{E^*}{\sqrt{C_L^*}}}{\left(\frac{E}{\sqrt{C_L}}\right)_{\max}} = \frac{\frac{1}{2 C_{D0}^{3/4} K^{1/4}}}{\frac{3^{3/4}}{4 C_{D0}^{3/4} K^{1/4}}} = \frac{2}{3^{3/4}} = 0.877$$

$$1 - 0.877 = 0.123 = 12.3\%$$